PRELIMINAR

Fiscal Rules for Commodity Exporters: Different Strokes for Different Folks?

Prepared by Carlos J. Garcia, Jorge E. Restrepo, and Evan Tanner¹

March 2009

Abstract

This paper compares welfare levels under alternative fiscal rules for small open commodity exporters whose fiscal income varies with the world commodity price (in a dynamic, stochastic, and general equilibrium model). Between the extremes of a procyclical balanced budget policy and an acyclical spending rule, there lies a continuum of rules. Thus, the best degree of spending stabilization is found. The acylical rule benefits households that do not enjoy access to capital markets by providing a financial cushion that they themselves cannot provide, boosting their mean consumption. However, households that enjoy full access to capital markets suffer under this rule, since the government reduces their role in smoothing consumption and accumulating assets.

JEL Classification Numbers: E32, E61, E62, E63, F41.

Keywords: Fiscal rules, welfare, small open economy, rule-of-thumb consumers. Authors' E-Mail Addresses: cgarcia@uahurtado.cl; jrestrepo@bcentral.cl; etanner@imf.org

¹ Garcia (corresponding author): Universidad Alberto Hurtado in Santiago Chile. Restrepo: Central Bank of Chile. Garcia and Restrepo: visiting scholars at the IMF Institute. Tanner: IMF Institute. We wish to thank Jordi Gali, Carlos Vegh, José de Gregorio, Selim Elekdag, two referees and seminar participants at the University of Chile, Central Bank of Chile, and the Catholic University of Chile. William Baeza helped code several simulations. All remaining errors are the authors' own.

Contents

Ι	Introduction	4
II.	The Model	8
	A. Households	9
	B. Firms	12
	C. Exports	16
	D. Aggregations	17
	E. Monetary Policy	17
	F. Fiscal Policy	18
	G. Market Clearing Conditions	20
III.	Calibration and Fynamics	24
IV.	Effects of a Commodity (Copper) Price Shock	23
V.	Calculation of Welfare Levels	29
	A. Methodology	29
	B. Results	30
VI.	Summary and Conclusions	36
Refe	erences	38
Tab	les	
1.	Baseline Parameters	23
Figu	ires	
1.	Volatility of the Commodity Price Growth and Government Spending Growth	5
2.	Volatility of GDP and Government Spending Growth	5
3.	Responses to a Price of Copper Shock	26
4.	Average of Simulated Series	28
5.	Welfare Gain (WG) and Variance of Copper Prices	31
6.	Variable Difference Between Regimes	32
7.	Difference of Welfare Gains as Measured in Consumption Units when Increases	
	[insert equations]	34
8.	Difference etc [insert full title]	34

I. INTRODUCTION

Most available evidence suggests that, in emerging/developing economies, fiscal policy is *procyclical* (Kaminsky, Reinhart, and Végh, (2004), Talvi and Végh, (2005)). Government consumption typically increases and taxes often fall during expansions, while the opposite often happens during recessions. Moreover, in countries whose exports are concentrated in one or a few primary resource-based commodities, government expenditures often move closely with the world prices of these exports. Thus, as Figure 1 suggests, in such countries, higher volatility of government spending is associated with higher commodity price volatility. Of course, past fiscal indiscipline may play a role in procyclical fiscal behavior. Procyclical spending cuts often occur not only when commodity prices fall, but also after a buildup of public debt. Moreover, as Figure 2 suggests, spending shocks often have broader spillover effects, insofar as higher volatility in government spending is typically linked to higher volatility in economic growth.²





Source: International Monetary Fund, United Nations and Saudi Arabian Monetary Agency; Major commodities by country are: Copper (Chile, Zambia), Soy (Paraguay), Gold (Peru, South Africa), Natural Gas and Oil (Iran). Oil (all other countries).

² In a related vein, Talvi, and Végh (2005) argue that pressures to increase public spending in countries that face large swings in their tax base, as is the case in many developing countries, are the cause of running a procyclical fiscal policy. Gavin et al (1996) and Gavin and Perotti (1997) have attributed this procyclical bias to the fact that developing countries are rationed from international credit markets in bad times.





Source: See Figure 1.

In this way, fiscal volatility may affect consumer welfare. For example, fiscal shocks may affect private consumption. Households that do not enjoy access to capital markets—"hand-to-mouth" or "non-Ricardian" households—are especially vulnerable in this aspect. Without their own financial buffer stocks, such households cannot smooth their consumption. Hence, when government spending falls, their disposable income and consumption fall with it. By contrast, households that do have access to capital markets—"Ricardian" optimizers—are better positioned to cushion themselves against such shocks.

Governments may wish to protect these more vulnerable "hand-to-mouth" households from fiscal volatility. Ideally, they would do so through a sequence of taxes and transfers whose magnitudes would yield exactly the hypothetical sequence of consumption by households if were in fact "Ricardian." However, such a policy may be difficult to implement, since the government may not know what household preferences are. As a more practical alternative, some commodity exporting countries have simply chosen to reduce fiscal volatility by implementing a *fiscal rule* that breaks the link between current commodity prices and public spending. While such rules may be ad-hoc in nature, they may be easier to communicate and implement than other more complicated policies (like the tax / transfer scheme).

The goal of this paper is to examine how both the level of government demand and its volatility affect consumer welfare. In our model, there are two sources of government revenue: lump-sum taxes (assumed to be constant) and export revenue from a resource-based commodity (in our model, copper) whose world-determined price fluctuates randomly. Government expenditures are assumed to be inherently useless; they appear in neither utility

nor production functions. Instead, the government merely functions as a conduit for mannalike commodity revenues. The government purchases both imports and domestic goods / services, which are ultimately supplied by households. (In this limited sense, government spending raises household income.)

When the government chooses among fiscal rules, it chooses how much to spend and when. Hence, a fiscal rule affects both the level and volatility of government spending. We emphasize several desirable characteristics of a fiscal rule. First, a fiscal rule should be transparent and easily understood. As Kydland and Prescott (1977) such a rule should bolster credibility. Second, the rule should reduce volatility and provide a precautionary cushion of assets for the most vulnerable (i.e. "hand-to-mouth") households. (The idea that the government should be a net creditor is not new; see for example Ayiagari, Marcet, Sargent, and Seppäla (2002)). Third, and in a related vein, the government's net asset position – debtor or creditor – must be bounded. The government's net creditor (or debtor) position should not grow without limit. ³

Arguably, a *balanced budget* rule is the easiest rule to understand: expenditures must always equal revenues. However, such a rule is inherently procyclical: it brings volatility that is detrimental to vulnerable households. By contrast, some countries (for example Chile (Figure 3) have opted for an *acyclical* (or *structural surplus*) rule in which expenditures are linked to *steady-state* (rather than current) commodity revenue.



Figure 3. Chile: Central Government Balance and Public Debt

Source: Ministry of Finance and Central Bank of Chile

³ This is related to, but not the same as, the "no-Ponzi game" condition which specifies that the *present value* of net assets must tend to zero.

In our model, average and steady state revenues exceed steady state consumption.⁴ Thus, over time, under the ascyclical rule, government will assume a creditor position. The net assets serve as an extra financial cushion for the "hand-to-mouth" households—a kind of publicly provided precautionary savings that such households are unable to provide for themselves. ⁵ However, under this policy, the government also reaps a 'dividend' that helps it to boost spending. In order to ensure that public asset growth is bounded, spending out of the dividend must equal or exceed a certain minimum ratio to net assets.

Under a balanced budget rule, spending fluctuates around a fixed mean. By contrast, under the acyclical rule, the government spends less in the early years and more later– and it does so on a smoother path. Also, these two types of rules are easily shown to be special cases of a more general fiscal rule – two specific points on a *continuum* of fiscal rules.

Welfare is measured in terms of steady-state consumption (Lucas, 1987, Schmitt-Grohé and Uribe, 2007; Bergin et al, 2007), and compared across regimes. Importantly, the source of cross-regime welfare differences should lie in both the mean of consumption (first moment) and its variability (second moment).

Traditionally, simulations in general equilibrium models have been based on first-order loglinear approximations which did not allow meaningful welfare comparisons under uncertainty (see for example Kim and Kim (2003)). As a remedy, we follow the literature using an algorithm developed by Schmitt-Grohé and Uribe (2004), whose second-order approximations permit us to assess the impact of policy-induced variability over other key economic variables, including consumption.⁶

The simulations reveal that some agents will prefer one rule over the other. As expected, macroeconomic aggregates are less volatile under the acyclical regime than under the

⁴ This feature is a consequence of the second order approximation that is performed; as Uribe and Schmitt-Grohe (2006) note, in such models, the mean of a variable rises with its variance.

⁵ Such an asymmetry generally presumes that there is an element of prudence (a non-zero third moment) in their utility function; see for example Carroll and Kimball (2006). A refinement of this argument is due to Huggett and Ospina (2001).

⁶ This type of approximation has been previously used to evaluate several issues, including the benefits of capital mobility and international risk sharing (Kim and Kim, (2003); the relative merits of fixed-versus-floating exchange rate regimes (Elekdag and Tchakarov, 2007; Bergin et al, 2007); optimal monetary and fiscal rules (Schmitt-Grohé and Uribe, 2007).

balanced budget regime, since expenditures follow a smoother path under former.⁷ This especially benefits the non-Ricardian consumers who are unable to smooth out volatility on their own.

By contrast, Ricardians are better off under the balanced budget regime. Since they have access to capital markets and they can do their own smoothing, public efforts to smooth are redundant. Moreover, Ricardian households, unlike non-Ricardian ones, can benefit from a stream of government spending that is higher (in the initial years) and more volatile. Only Ricardians can save: they smooth their consumption stream and build up assets that fund higher consumption in the outer years. We also find that Ricardians are not indifferent to the level of "dividend" spending under an acyclical regime. When the government raises the dividend spending ratio, agents sell more to the government in the initial years. When the government in the outer years. Our analysis shows that, under an acyclical regime, there is a critical ratio of dividend spending at which these two effects are balanced out, maxizing welfare level for Ricardians under the acyclical regime.

The remainder of the paper is organized as follows. In Section II, we present the model in its entirety. In Section III, we discuss the calibration of the parameters, present the simulation results and analyze the models' dynamics. In Section IV, we present the welfare analysis. Finally in Section V we summarize and conclude.

II. THE MODEL

Our New Keynesian model most closely resembles one developed by Smets and Wouters (2002), but also draws on work by Woodford (2003), Clarida et al (1999), and Galí et al (2007). However, our model of a small open economy also includes: hand-to-mouth consumers (as in Galí et al (2007), capital and investment with adjustment costs, raw materials, government, Greenwood, Hercowitz and Huffman (GHH 1988) preferences and a representative "Ricardian" agent (rather than overlapping generations). Our structure also follows Gali and Monacelli's (2005) model of a representative agent with two goods (domestic and foreign) by using constant elasticity of substitution (CES) consumption baskets and price stickiness à la Calvo (1983). We close the small open economy by introducing a risk premium, following Schmitt-Grohé and Uribe (2003). Another essential reference among recent models for emerging economies is the general equilibirium model (GEM, Laxton and Pesenti, 2003). They have a very complex and more realistic structure to

⁷ Also, under the acyclical rule, the government saves the windfalls. In so doing, it avoids some of the undesired currency appreciation—a Dutch disease that typically plagues noncommodity exporters.

describe the relationship between final goods, intermediate goods and raw and semi finished materials.⁸

A. Households

We assume a continuum of infinitely lived households indexed by $i \in [0,1]$. Following Galí et al. (2007), a fraction of households λ consume their current labor income; they do not have access to capital markets and hence neither save nor borrow. Such agents have been termed "hand-to-mouth" consumers. The remainder $1 - \lambda$ save, have access to capital markets, and are able to smooth consumption. Therefore, their intertemporal allocation between consumption and savings is optimal (Ricardian or optimizing consumers). Both segments optimize on the intratemporal margin in labor markets.

Consumption by Ricardian Households

The representative household maximizes expected utility

$$E_o \sum_{t=0}^{\infty} \beta^t U \Big(C_t^o(i), N_t^o(i) \Big), \tag{1}$$

subject to the budget constraint

$$P_{t}C_{t}^{o}(i) = W_{t}(i)N_{t}^{o}(i) + B_{t}^{o}(i) - S_{t}B_{t}^{o^{*}}(i) + D_{t}^{o}(i) - P_{t}T_{t} - R_{t}^{-1}B_{t+1}^{o}(i) + S_{t}(\Phi(B_{t}^{*})R_{t}^{*})^{-1}B_{t+1}^{o^{*}}(i),$$
(2)

where $C_t^o(i)$ is consumption, $D_t^o(i)$ are dividends from ownership of firms, $\Phi(B_t^*)$ is the country risk premium, S_t is the nominal exchange rate, $B_t^{o^*}(i)$ denotes private net foreign assets, where we define a positive value of $B_t^{o^*}(i)$ as debt, $W_t(i)$ is nominal wage, $N_t^o(i)$ is the number of hours of work, $B_t^{o^*}(i)$ is government debt held by households, R_t and R_t^* are the gross nominal return on domestic and foreign assets (where $R_t = 1 + i_t$ and $R_t^* = 1 + i_t^*$) and T_t are lump-sum taxes.

Our utility function (Correia et al, 1995) yields realistic values for consumption volatility:

$$U(C,N) = \frac{(C - \psi N^{\phi})^{1-\sigma} - 1}{1 - \sigma}.$$
 (3)

⁸ Also, Laxton and Pesenti assume habit formation in consumption, a different price setting, nontradable goods and adjustment costs for the demand of imports and nontradable goods.

Note that $1/\sigma$ is the intertemporal elasticity of substitution in consumption and $1/(\varphi - 1)$ is the elasticity of labor supply to wages. The value of ψ is calibrated to obtain a realistic fraction of steady state hours worked. Note also that the rate of relative prudence is $(C_t^0(i) - \psi N_t^0(i)^{\varphi}) U_{CCC} / U_{CC} = -(1 + \sigma)$. This statistic is important to explain precautionary savings -- one of the most important results of this article. As other authors have noted (Carroll and Kimball (2006)), for any individual agent, unless this statistic is non-zero, the level of consumption (and hence savings) will be invariant to volatility. The first-order condition for consumption is:

$$\left(C_{t}^{0}(i) - \psi N_{t}^{0}(i)^{\varphi}\right)^{-\sigma} = \beta E_{t}\left(\left(C_{t+1}^{0}(i) - \psi N_{t+1}^{0}(i)^{\varphi}\right)^{-\sigma} R_{t}\left(\frac{P_{t}}{P_{t+1}}\right)\right)$$
(4)

From the first order conditions it is also possible to derive the interest parity condition:

$$\frac{S_{t}}{P_{t}} = E_{t} \left[\left(\frac{S_{t+1}}{P_{t+1}} \right) \frac{R_{t}^{*} \Phi\left(B_{t}^{*}\right)}{R_{t} \left(\frac{P_{t}}{P_{t+1}}\right)} \right]$$
(5)

Consumption by Hand-to-Mouth Households

For "Non-Ricardian" households, utility is:

$$U(C_t^r(i), N_t^r(i)). (6)$$

We assume that these households neither save nor borrow (Mankiw (2000)). As a result, their level of consumption is given by their disposable income:

$$P_{t}C_{t}^{r}(i) = W_{t}(i)N_{t}^{r}(i) - P_{t}T_{t}.$$
(8)

Labor Supply

Symmetric with the goods markets (discussed below), the continuum of monopolistically competitive households supply a differentiated labor service to the intermediate-goods-producing sector and a labor aggregator combines as much household-labor as is demanded by firms, with a constant-returns technology. The aggregate labor index has the CES form:

$$N_{t} = \left[\int_{0}^{1} N_{t}(i)^{\frac{1}{1+\theta_{\omega}}} di\right]^{1+\theta_{w}}$$
(9)

where N_t (*i*) is the quantity of labor used from each household. The representative labor aggregator minimizes the cost of producing a chosen amount of the aggregate labor index, given each household's wage rate W_t (*i*). Then, she sells units of labor index at their unit cost W_t (with no profit), to the production sector:

$$W_{t} = \left[\int_{0}^{1} W_{t}(i)^{-\frac{1}{\theta_{\omega}}} di\right]^{-\theta_{\omega}}$$
(10)

Note that, while prices are sticky, wages are completely flexible. Nominal wages are set by households so as to maximize their intertemporal objective function (1) subject to the intertemporal budget constraint (2) and to the total demand for their labor services, which is given by:

$$N_t(i) = \left[\frac{W_t(i)}{W_t}\right]^{-\frac{1+\theta_{\omega}}{\theta_{\omega}}} N_t$$
(11)

As a result the supply of each household is given by

$$W_t(i) = (1 + \theta_w) \varphi \psi N_t(i)^{\varphi - 1}$$
(12)

where $(1 + \theta_w)$ is a mark-up over the current ratio of the marginal disutility of labor and the marginal utility of an additional unit of consumption. For rule-of-thumb households, wages are set at the average wage level of optimizing households.

Demand for Domestic and Imported Consumption Goods

Consumption is a CES aggregate of consumption of domestic $C_t^D(i)$ and imported goods $C_t^F(i)$, where η_C is the elasticity of substitution between domestic and foreign goods and α_C is the steady-state share of imported goods in total consumption:

$$C_{t} = \left(\alpha_{c} \frac{1}{\eta_{c}} \left(C_{t}^{D}\right)^{\frac{\eta_{c}-1}{\eta_{c}}} + \left(1 - \alpha_{c}\right)^{\frac{1}{\eta_{c}}} \left(C_{t}^{F}\right)^{\frac{\eta_{c}-1}{\eta_{c}}}\right)^{\frac{\eta_{c}}{\eta_{c}-1}}$$
(13)

The demand for each set of differentiated domestic and imported goods, as derived from expenditure minimization, is:

$$C_t^D = \alpha_c \left(\frac{P_t^D}{P_t}\right)^{-\eta_c} C_t \tag{14}$$

$$C_t^F = (1 - \alpha_c) \left(\frac{P_t^F}{P_t}\right)^{-\eta_c} C_t$$
(15)

A weighted average of either domestic or imported differentiated goods composes each type of good, which also consists of a Dixit-Stiglitz index:

$$C_t^K = \left(\int_0^1 C_t^K(j)^{\frac{\varepsilon_K - 1}{\varepsilon_K}} dj\right)^{\frac{\varepsilon_K}{\varepsilon_K - 1}}.$$
 (16)

$$C_t^K(j) = \left(\frac{P_t^K(t)}{P_t^K}\right)^{-\varepsilon_K} C_t^K.$$
(17)

for K= D (domestic) and F (foreign). $P_{t..}$ the aggregate consumer price index or CPI is defined as:

(18)
$$P_t = \left(\alpha_c (P_t^D)^{1-\eta_c} + (1-\alpha_c)(P_t^F)^{1-\eta_c}\right)^{\frac{1}{1-\eta_c}}$$

where the respective price index is:

$$P_t^K = \left(\int_0^1 P_t^K(j)^{1-\varepsilon_K} dj\right)^{\frac{1}{1-\varepsilon_K}}$$
(19)

where K = D (domestic), F (foreign).

B. Firms

Domestic intermediate-goods firms

We assume a continuum of monopolistically competitive firms, indexed by $j \in [0,1]$ producing differentiated intermediate goods. The production function of the representative intermediate-good firm, indexed by (*j*) corresponds to a CES combination of capital $K_t(j)$ and labor $N_t(j)$, to produce $Y_t^D(j)$ and is given by:

$$Y_t^D(j) = A_t \left[\alpha K_t(j)_t \frac{\sigma_s - 1}{\sigma_s} + (1 - \alpha) N_t \frac{\sigma_s - 1}{\sigma_s}(j) \right]^{\frac{\sigma_s}{\sigma_s - 1}}$$
(20)

where A_t the technology parameter, and $\sigma_{s..}$ the elasticity of substitution between capital and labor, are both greater than zero.

The firms' costs are minimized taking as given the rental price of capital, R_t^k and the wage, W_t subject to the production function (technology). The relative factor demands are derived from the first-order conditions:

$$\frac{R_t^k}{W_t} = \left(\frac{\alpha}{1-\alpha}\right) \left(\frac{N_t(j)}{K_t(j)}\right)^{\frac{1}{\sigma_s}}$$
(21)

Thus, marginal cost is given by:

$$MC^{D} = \frac{1}{A_{t}} \left[\alpha^{\sigma_{s}} (R_{t}^{k})^{1-\sigma_{s}} + (1-\alpha)^{\sigma_{s}} (W_{t})^{1-\sigma_{s}} \right]^{\frac{1}{1-\sigma_{s}}}$$
(22)

When firm (j) receives a signal to optimally set a new price à la Calvo (1983), it maximizes the discounted value of its profits, conditional on the new price:

$$\max\sum_{k=0}^{\infty} \theta_D^k E_t \left\{ \Lambda_{t,t+k} Y_{t+k}^D(j) (P_t^{D^*}(j) - MC_{t+k}^D) \right\}$$
(23)

subject to:

$$Y_{t+k}^{D}(j) \le \left(\frac{P_t^{D^*}(j)}{P_t^{D}}\right)^{-\varepsilon_D} Y_{t+k}^{D}$$
(24)

Where the probability that a given price can be reoptimized in any particular period is constant and is given by $(1 - \theta_D)$ and ε_D is the elasticity of substitution between any two differentiated goods. $P_t^{D^*}$ must satisfy the first order condition:

$$\sum_{k=0}^{\infty} \theta_D^k E_t \left\{ \Lambda_{t,t+k} Y_{t+k}^D(j) \left(P_t^{D^*}(j) - \frac{\varepsilon_D}{\varepsilon_D - 1} M C_{t+k}^D \right) \right\} = 0$$
(25)

where the discount factor $\Lambda_{t,t+k}$ is:

$$\Lambda_{t,t+k} = \beta^k \left(\frac{C_{t+k}^0}{C_t^0} \right)^{-\sigma} \left(\frac{P_t}{P_{t+k}} \right).$$

Firms that did not receive the signal will not adjust their prices. Those who do reoptimize choose a common same price, $P_t^{D^*}$. Finally, the dynamics of the domestic price index P_t^D is described by the equation:

$$P_{t}^{D} = \left[\theta_{D}(P_{t-1}^{D})^{1-\varepsilon_{D}} + (1-\theta_{D})(P_{t}^{D^{*}})^{1-\varepsilon_{D}}\right]^{\frac{1}{1-\varepsilon_{D}}}$$
(26)

Intermediate-goods importing firms

As in the domestic sector, price setting in the import sector reflects little exchange rate passthrough in the short run (as in Monacelli, 2005, and Smets and Wouters, 2002). Such an assumption, while simplistic, provides realistic simulations (impulse response functions). This sector consists of firms that import a homogenous good from abroad and turn it into a differentiated foreign good for the home market using a linear production technology. Import firms are only allowed to change their price when they receive a random price-change signal. Thus, the dynamics of the import price index is also described by an equation similar to (24). But in this case, firms reset their price in response to variations in the exchange rate or the foreign price; they optimally charge the import price abroad expressed in domestic currency.

$$P_t^F = \left[\theta_F (P_{t-1}^F)^{1-\varepsilon_F} + (1-\theta_F)(S_t P_t^{F^*})^{1-\varepsilon_F}\right]^{\frac{1}{1-\varepsilon_F}}$$
(27)

Note $(1 - \theta_F)$ and ε_F have the same definition as before but here they apply to the intermediate-goods importing firms.

Final goods distribution

Total final output is expressed with a CES aggregator function (across firms). There is a perfectly competitive aggregator, which distributes the final good using a constant return to scale technology. It is valid for both K=D (domestic) and F (imported) goods:

$$Y_{t}^{K} = \left(\int_{0}^{1} Y_{t}^{K}(j)^{\frac{\varepsilon_{K}-1}{\varepsilon_{K}}} dj\right)^{\frac{\varepsilon_{K}}{\varepsilon_{K}-1}}$$
(28)

 $Y_t^K(j)$ is the quantity of the intermediate good (domestic or imported) included in the bundle that minimizes the cost of any amount of output Y_t . The aggregator sells the final good at its unit cost P_t with no profit:

$$P_t^K = \left(\int_0^1 P_t^K(j)^{1-\varepsilon_K} dj\right)^{\frac{1}{1-\varepsilon_K}}$$
(29)

where P_t is the aggregate price index. Finally, demand for any good $Y_t^K(j)$ depends on its price P(j), which is taken as given, relative to the aggregate price level P_t :

$$Y_{t}^{K}(j) = \left(\frac{P(j)}{P_{t}}\right)^{-\varepsilon_{K}} Y_{t}^{K}$$
(30)

Optimizing investment firms and Tobin's Q

There are firms that produce homogenous capital goods and rent them to the intermediategoods firms. Firms are owned exclusively by Ricardian households. Firms invest the amount so as to maximize firm value:

$$V^{t}(K_{t}^{o}) = R_{t}^{k}K_{t}^{o} - P_{t}^{I}I_{t}^{o} + E_{t}(V^{t+1}(K_{t+1}^{o}))$$
(31)

subject to a capital accumulation constraint that includes an adjustment cost function $\phi(.)$.

$$K_{t+1}^{o} = (1 - \delta)K_{t}^{o} + \phi \left(\frac{I_{t}^{o}}{K_{t}^{o}}\right)K_{t}^{o}$$
(32)

The first-order conditions are:

$$Q_t^o \phi' \left(\frac{I_t^o}{K_t^o} \right) - \frac{P_t^D}{P_t} = 0$$
(33)

$$Q_{t}^{o} = E_{t} \left\{ \frac{1}{R_{t}} \left(\frac{P_{t+1}}{P_{t}} \right) \left[\frac{R_{t+1}^{k}}{P_{t+1}} + Q_{t+1}^{o} \left((1-\delta) + \phi_{t+1} - \frac{I_{t+1}^{o}}{K_{t+1}^{o}} \phi_{t+1}^{'} \right) \right] \right\}$$
(34)

Equation (35) corresponds to Tobin's Q: the marginal cost of an additional unit of investment should be equal to the present value of the marginal increase in equity that it generates.

Demand for investment goods

Overall investment is equal to a CES aggregate of domestic and imported goods. Where η_I is the elasticity of substitution between domestic and foreign goods and α_I is the steady-state share of domestic goods in total investment.

$$I_{t} = \left(\alpha_{I}^{\frac{1}{\eta_{I}}} (I_{t}^{D})^{\frac{\eta_{I}-1}{\eta_{I}}} + (1-\alpha_{I})^{\frac{1}{\eta_{I}}} (I_{t}^{F})^{\frac{\eta_{I}-1}{\eta_{I}}}\right)^{\frac{\eta_{I}}{\eta_{I}-1}}$$
(35)

Demand for investment goods, domestic and imported respectively, is derived from expenditure minimization, namely:

$$I_t^D = \alpha_I \left(\frac{P_t^D}{P_t^I}\right)^{-\eta_I} I_t$$
(36)

$$I_t^F = (1 - \alpha_I) \left(\frac{P_t^F}{P_t^I}\right)^{-\eta_I} I_t$$
(37)

A weighted average bundle of either domestic or imported differentiated goods thus comprises each type of investment good (a Dixit-Stiglitz index):

$$I_{t}^{K} = \left(\int_{0}^{1} I_{t}^{K}(j)^{\frac{\varepsilon_{K}-1}{\varepsilon_{K}}} dj\right)^{\frac{\varepsilon_{K}}{\varepsilon_{K}-1}}$$
(38)

$$I_t^K(j) = \left(\frac{P_t^K(j)}{P_t^K}\right)^{-\varepsilon_K} I_t^K$$
(39)

for k=D, F. The aggregate price of investment (investment deflator) is defined as:

$$P_{t}^{I} = \left(\alpha_{I}(P_{t}^{D})^{1-\eta_{I}} + (1-\alpha_{I})(P_{t}^{F})^{1-\eta_{I}}\right)^{\frac{1}{1-\eta_{I}}}$$
(40)

Each composite good is itself a bundle of differentiated goods

C. Exports

The demand for total domestic (non-copper) exports from foreign countries is:

$$X_t^D = \left(\int_0^1 X_t^D(j)^{\frac{\varepsilon_D - 1}{\varepsilon_D}} dj\right)^{\frac{\varepsilon_D}{\varepsilon_D - 1}}$$
(41)

Exports of good J depend on its own relative price:

$$X_t^D(j) = \left(\frac{P_t^D(j)}{P_t^D}\right)^{-\varepsilon_D} X_t^D$$
(42)

There is a demand for each set of differentiated domestic goods, which in turn depends on both total consumption abroad and on the home price of domestic goods (relative to its price in the foreign country):

$$X_t^D = \left[\left(\frac{P_t^D}{S_t P_t^{D^*}} \right) \right]^{-\eta^*} C_t^{D^*}$$
(43)

D. Aggregation

Total consumption is a weighted sum of consumption by Ricardian and rule-of-thumb agents:

$$C_t = \lambda C_t^r + (1 - \lambda)C_t^o = \int_0^\lambda C_t^r(i)di + \int_\lambda^1 C_t^o(i)di$$
(44)

Since only Ricardian households invest and accumulate capital, total investment is equal to $(1 - \lambda)$ times optimizing investment:

$$I_t = (1 - \lambda)(I_t^o) \tag{45}$$

Likewise, the aggregate capital stock is:

$$K_t = (1 - \lambda)(K_t^o) \tag{46}$$

Again, only optimizing households hold financial assets:

$$B_t = (1 - \lambda)(B_t^o) \tag{47}$$

Foreign assets (or debt) include fiscal $B_t^{G^*}$ and private held assets $B_t^{O^*}$:

$$B_t^* = B_t^{G^*} + (1 - \lambda)B_t^{o^*}$$
(48)

Hours worked are given by a weighted average of labor supplied by each type of consumer:

$$N_t = \lambda N_t^r + (1 - \lambda) N_t^o \tag{49}$$

Finally, in equilibrium each type of consumer works the same number of hours:

$$N_t = N_t^r = N_t^o \tag{50}$$

E. Monetary policy

Even while this paper focuses on fiscal policy, price stability requires there also be an active central bank. Thus, in abbreviated way, we also include monetary policy: the central bank sets the nominal interest rate according to the following rule:

$$R_{t} = \overline{R} \left(\left(\frac{\Pi_{t}}{\overline{\Pi}} \right)^{\phi_{\pi}} \left(\frac{YR_{t}}{\overline{YR}_{t}} \right)^{\phi_{y}} \right)$$
(51)

where \overline{R} is the steady state nominal interest rate, Π_t is total inflation, $\overline{\Pi}$ is steady state total inflation (assumed to be zero), YR_t is GDP without the natural resource and \overline{YR} is steady state value.

F. Fiscal Policy

The government budget constraint is:

$$IT_{t} + R_{t}^{-1}B_{t+1}^{G} + S_{t}(\Phi(B_{t+1}^{*})R_{t}^{*})^{-1}B_{t+1}^{G*} = B_{t}^{G} + S_{t}B_{t}^{G*} + P_{t}^{G}G_{t}$$
(52)

where IT_t is total revenue (copper and otherwise), B_t^G is domestic public debt, $S_t B_t^{G^*} = v_b B_t^G$ is public foreign debt (a fixed proportion of domestic public debt) and $P_t^G G_t$ is public spending.

There are two sources of revenue: a domestic (non-copper) lump-sum tax $P_t T_t$ and copper revenue $\tau_{cu} (S_t P_t^{cu} Q^{cu})$ where τ_{cu} is the share of the production of the natural resource (copper) owned by the government, P_t^{cu} is the world price of copper, and Q^{cu} is the

quantity supplied (assumed to be constant). Importantly, copper revenue is essentially "manna from heaven." The government purchases goods and services with this manna.

Hence, non-commodity revenues are assumed to always be in steady state: $P_tT_t = \overline{PT}, \forall t$. By contrast, copper prices are assumed to have a positive variance.

Simple fiscal rules

This paper highlights *fiscal rules* that meet several criteria. The rule should be transparent and easily understood, as Kydland and Prescott (1977) emphasized. And, the government's net asset position – debtor or creditor – must be bounded. Neither net debt nor assets may grow without limit.

Our benchmark is a *balanced-budget* (BB) rule:

$$P_t^G G_t(BB) = IT_t - \widetilde{R}_t B_t^G$$
(53a)

where \tilde{R}_t is a weighted average (effective) interest rate on total debt (domestic plus foreign), namely:

$$\widetilde{R}_{t} \equiv \left[\frac{R_{t}-1}{R_{t}} + \frac{R_{t}^{*}\Phi(B_{t+1}^{*})-1}{R_{t}^{*}\Phi(B_{t+1}^{*})}v_{b}\right]$$

While transparency is a subjective criterion, most would agree that a balanced budget rule is easy to understand. Also, by definition, government debt is bounded at a constant (zero) level under this rule.

However a drawback of this rule is that it exposes vulnerable consumers to market (copper price) volatility. We thus propose an alternative acyclcical (*AC*) or structural balance rule that provides a cushion against market volatility – especially for the non-Ricardian (or "hand-to-mouth") consumers who are unable to smooth their consumption stream. Under this rule, spending is linked one-to-one with steady-state (or structural - permanent) government revenues less interest payments, but with a small adjustment factor for the debt level (μ_x). Formally, this rule is written:

$$P_t^G G_t(AC) = \overline{IT} - \left[\tilde{R}_t + \mu_x\right] B_{t+1}^G$$
(53b)

While AC rule is somewhat more complicated than the balanced-budget rule, it too might be easily communicated to the public: government spending should be, at least at the beginning, equal to permanent revenues less a small structural surplus κ -- precautionary savings for bad times.

Are public assets bounded under this rule? To investigate conditions under which the government's creditor position is bounded, consider a simplified case with no foreign debt $(B_t^{G^*} = 0, \forall t \text{ and } v_b = 0)$. Equation (52) is thus:

$$R_t^{-1}B_{t+1}^G = B_t^G + P_t^G G_t - IT_t$$

Substituting this equation (budget constraint) in the fiscal rule (53b), noting that, in this special case, $\widetilde{R_t} \equiv (R_t - 1)/R_t$, and rearranging, we see that debt evolves between any two periods, t and t+1 according to:

$$B_{t+1}^{G}(AC) = \left(1 - R_{t}\mu_{x}\right)B_{t}^{G}(AC) + R_{t}\left(\overline{IT} - IT_{t}\right)$$

This equation converges if only if $0 < |1 - R\mu_x| < 1.^9$ The next task is to see how debt evolves over an infinite horizon:

Doing so requires some simplifying assumptions: for all periods, $R_t = R \ \forall t$. In this case, over a z-period horizon,

The (negative) debt level converges to the *annuity value* of the government's primary surpluses over an infinite horizon - κ / μ_x as long as $\mu_x < R^{-1}$ and hence $0 < [1 - R\mu_x] < 1$.¹⁰

$$B_{t+1}^G = B_t^G \tag{53c}$$

In this case, if copper prices equal their steady state value $[\overline{\tau_{cu}SP^{cu}Q^{cu}} = \tau_{cu}(S_tP_t^{cu}Q^{cu})]$, total government debt stays constant. If there is an adverse shock to copper prices and $\mu_x = 0$, the level of debt will go up to the point where revenues and expenditures are once again equated. Put differently, if $\mu_x = 0$, government debt follows a random walk: the debt will remain at its new level forever unless there is another shock. Thus, the model will not converge if $\mu_x = 0$.

¹⁰ As a related issue, μ_x must be non-zero. Otherwise, government debt follows a random walk. To see this, consider a special case where $\mu_x = 0$ and v = 0 (no foreign debt):

⁹ As a related issue, μ_x must be non-zero. Otherwise, government debt follows a random walk. To see this, consider a special case where $\mu_x = 0$ and v = 0 (no foreign debt):

What determines the behavior of public debt with the acyclical rule?

If we take expectation of the last expression, we get:

$$E_t\left(B_{t+1}^G(AC)\right) = B_t^G(AC) - E_t\left(R_t\right)\mu_x B_t^G(AC)$$

on B_{t+1}^* . In

But $E(R_t)$ depends

Appendix XX, we show the economy face an asymmetry in the risk premium i.e. interest rates increase with debt level. Therefore $E(B_{t+1}^G(AC))\langle 0 \rangle$ provides a buffer against this asymmetry. In other words, if government wants to have a structural balance rule that provides a cushion against market volatility, it needs to have this buffer against the asymmetry that produces the risk premium in the economy.

Our simulations of the AC rule confirm this intuition. For the initial periods, we find that the government expenditure is smaller than in the future. This feature of the simulation is consistent with Schmitt-Grohé and Uribe (2004), who note that, in models that use second-order approximations (like this one), the variances of the variables have an impact on its mean values.

What determines κ ? In Appendix XX, we show that $\kappa \ge 0$. We also show that κ increases with the variability of copper prices (tax revenues). Such a result must be the case if the country wishes to set a precise target for spending: Under the *AC* regime, expenditures can be explained by two components: steady state tax revenues \overline{IT} and a "dividend" term div_t -- the increment that the government spends (saves) as a result of its creditor (debtor) position:

$$P_{t+Z}{}^{G}G_{t+Z}(AC, avg) < \overline{IT} + div_{t}$$

where

$$div_{t} = \left[\tilde{R} + \mu_{x}\right] \left[\kappa^{*} \sum_{z=1}^{Z} (1 - R\mu_{x})^{z-1}\right]$$

$$B_{t+1}^{G} = B_{t}^{G}$$
(53c)

In this case, if copper prices equal their steady state value $[\overline{\tau_{cu}SP^{cu}Q^{cu}} = \tau_{cu}(S_tP_t^{cu}Q^{cu})]$, total government debt stays constant. If there is an adverse shock to copper prices and $\mu_x = 0$, the level of debt will go up to the point where revenues and expenditures are once again equated. Put differently, if $\mu_x = 0$, government debt follows a random walk: the debt will remain at its new level forever unless there is another shock. Thus, the model will not converge if $\mu_x = 0$.

We may thus think of $R_t \mu_x$ as a "dividend ratio." For a *z*-period finite horizon, average expenditures under the *AC* rule are:

$$P_{t+Z}{}^{G}G_{t+Z}(AC) = \overline{IT} + (\sum_{z=0}^{Z} div_{t})/Z$$

So long as the bounds criterion is satisfied, over an infinite horizon, the dividend converges to:

$$\lim_{z\to\infty} div_{t+z} = (1 + \mu_k / R)\kappa\mu_k$$

Thus, under the AC regime, average value of government expenditures converges to steadystate revenue (lump sum and copper) plus the long-run dividend.

The effect of a increase in μ_k on average expenditures is ambiguous. Such an effect depends on whether the government a debtor ($B^G > 0$) or a creditor ($B^G < 0$). However, in either case, changing μ_x changes the time profile (now versus later) of government expenditures.

For the debtor case ($B^G > 0$), an increase in μ_x reduces government expenditures and speeds up the drawdown of government debt.

However, the creditor case ($B^G < 0$) is more relevant for our analysis, since we assume that the government starts off with zero debt and accumulates assets thereafter. In this case, an increase in μ_x helps to push up government expenditures now. But, since raising μ_x slows down the build up of the government's "war chest" it reduces the annuity value thereof --- κ/μ_x falls – and hence reduces government expenditures in the long term.

A more general fiscal rule

It may be easily seen that rules BB and AC are merely two options along a continuum of a general rule (GR) whose form is:

$$P_t^G G_t(GR) = \overline{IT} - \left[\widetilde{R}_t + \mu_x\right] B_t^G + \alpha_r(IT_t - \overline{IT})$$

Thus, for *BB*, $\alpha_{\gamma} = 1, \mu_x = 0$; for an *AC* regime, $\alpha_{\gamma} = 0$, and $0 < \mu_x < R^{-1}$. For other intermediate rules, $0 < \alpha_{\gamma} < 1$, and $0 < \mu_x < R^{-1}$. We may thus think of alternative pairings of

 $[\alpha_{\gamma}, \mu_{x}]$ as ways of introducing both the mean and variance of government spending in a continuous fashion.

Government demand for domestic and imported goods

The government demands domestic and imported goods, according to:

$$G_{t} = \left(\alpha_{G}^{\frac{1}{\eta_{G}}}(G_{t}^{D})^{\frac{\eta_{G}-1}{\eta_{G}}} + (1-\alpha_{G})^{\frac{1}{\eta_{G}}}(G_{t}^{F})^{\frac{\eta_{G}-1}{\eta_{G}}}\right)^{\frac{\eta_{G}-1}{\eta_{G}-1}}$$
(55)

where η_G is the elasticity of substitution between domestic and foreign goods and α_G is the steady-state share of domestic goods in total government expenditure.

The demand for domestic and imported goods derived from expenditure minimization is given by:

(56)
$$G_{t}^{D} = \alpha_{G} \left(\frac{P_{t}^{D}}{P_{t}^{G}}\right)^{-\eta_{G}} G_{t}$$
$$G_{t}^{F} = (1 - \alpha_{G}) \left(\frac{P_{t}^{F}}{P_{t}^{G}}\right)^{-\eta_{G}} G_{t}$$
(57)

Each type of good (domestic, imported) consumed by the government is composed of a weighted average of differentiated goods, which also consists of a Dixit-Stiglitz index:

$$G_{t}^{K} = \left(\int_{0}^{1} G_{t}^{K}(j)^{\frac{\varepsilon_{K}-1}{\varepsilon_{K}}} dj\right)^{\frac{\varepsilon_{K}}{\varepsilon_{K}-1}}$$
(58)

$$G_t^K(j) = \left(\frac{P_t^K(j)}{P_t^K}\right)^{-\varepsilon_K} G_t^K$$
(59)

for K=D (domestic), F (foreign). The aggregate price deflator of government spending is:

$$P_t^G = \left(\alpha_G (P_t^D)^{1-\eta_G} + (1-\alpha_G) (P_t^F)^{1-\eta_G}\right)^{\frac{1}{1-\eta_G}}$$
(60)

Domestic and imported goods are themselves bundles of differentiated goods

Welfare implications of alternative fiscal rules: what should we expect from simulations?

Results of model simulation are presented below in Section V. In this, we compare welfare levels between BB and AC for Ricardian and non-Ricardian consumers. We "fine tune" such comparisons by also examining $[\alpha_{\gamma}, \mu_{x}]$ over a continuum of values. However, there are some impacts of the choice of fiscal rule that are quite intuitive and easy to see.

Implication (1): Welfare for both types of consumers will increase when government expenditures increase. This implication is uncontroversial. It simply reflects the fact that the government has an exclusive right to spend its manna from heaven (copper revenues) when it chooses (according to the rule). More spending raises the demand for domestic (as well as imported) goods and services, whose ultimate suppliers are the economy's households – both Ricardian and non-Ricardian.

Implication (2): *Discounted welfare for both types of consumers will increase when the time profile of government expenditures is shifted towards the present*. As before, this implication is simply a consequence of the government's distribution rights for manna (copper). More spending now raises the demand for goods and services supplied by the economy's households – now.

Implication (3): Reducing the variance of government expenditures helps non-Ricardian consumers more than Ricardian ones; the latter are able to smooth their consumption stream on their own.

Implication (4): *Reducing the variance of government expenditures reduces asset accumulation by Ricardian consumers.* In a smoother environment (AC versus BB), Ricardians have less incentive to save on a precautionary basis. This implication is not necessarily bad for Ricandian consumers. Extra saving could also be costly in terms of welfare.

Implication (5): For these reasons, it is expected that non-Ricardians will prefer AC over BB while (based on the first two implication) Ricardians might prefer BB over AC.

G. Market-Clearing Conditions

The factor market-clearing conditions are total employment by all firms j:

$$N_t = \int_0^1 N_t(j) dj \tag{61}$$

and full capital utilization

$$K_{t} = \int_{0}^{1} K_{t}(j) dj$$
 (62)

The good market-clearing condition is:

$$Y_{t}^{D}(j) = (C_{t}^{D}(j) + I_{t}^{D}(j) + G_{t}^{D}(j) + X_{t}^{D}(j))$$
(63)

Using equation (17) and (30), (39), (43) and (59), we obtain:

$$Y_{t}^{D}(j) = \left(\frac{P_{t}^{D}(j)}{P_{t}^{D}}\right)^{-\varepsilon_{D}} \left(C_{t}^{D} + I_{t}^{D} + G_{t}^{D} + X_{t}^{D}\right)$$
(64)

Equation (64) should be plugged into equation (28), which is:

$$Y_t^K = \left(\int_0^1 Y_t^K(j)^{\frac{\varepsilon_K - 1}{\varepsilon_K}} dj\right)^{\frac{\varepsilon_K}{\varepsilon_K - 1}}$$

for K=,D, F. In turn, this yields

$$Y_{\iota}^{D} = \left[\int_{0}^{1} \left(\frac{P_{\iota}^{D}(j)}{P_{\iota}^{D}}\right)^{-\varepsilon_{D}} \left(C_{\iota}^{D} + I_{\iota}^{D} + G_{\iota}^{D} + X_{\iota}^{D}\right)^{\frac{\varepsilon_{D}-1}{\varepsilon_{D}}} dj\right]^{\frac{\varepsilon_{D}}{\varepsilon_{D}}-1}$$

Adding up and simplifying yields the symmetric equilibrium for the domestic market:

$$Y_{t}^{D} = (C_{t}^{D} + I_{t}^{D} + G_{t}^{D} + X_{t}^{D})$$
(65)

where the total supply of domestic goods equals total demand of the domestic produced good for consumption, investment, government spending and exports. Finally, the economy-wide budget identity can be expressed as:

$$P_{t}C_{t} = -P_{t}^{G}G_{t} - P_{t}^{I}I_{t} + P_{t}^{D}Y_{t}^{D} + (P_{t}^{F}Y_{t}^{F} - S_{t}P_{t}^{*F}Y_{t}^{F}) + S_{t}\left(\Phi\left(B_{t}^{*}\right)R_{t}^{*}\right)^{-1}B_{t+1}^{*} - S_{t}B_{t}^{*} + \tau_{cu}(S_{t}P_{t}^{cu}Q^{cu})$$
(66)

Equation (66) has an intuitive interpretation. First note that GDP is the (approximately) sum of domestically produced goods plus value added on the distribution of imports, plus copper exports: ¹¹

$$P_{t}Y_{t} = P_{t}^{D}Y_{t}^{D} + (P_{t}^{F}Y_{t}^{F} - S_{t}P_{t}^{*F}Y_{t}^{F}) + (S_{t}P_{t}^{cu}Q^{cu})$$
(67)

Thus, according to the national income accounting identity, consumption must equal GDP minus investment (I) and government expenditures G plus foreign debt (positive values of B_t^*), which is written:

$$S_{t}\left(\Phi\left(B_{t}^{*}\right)R_{t}^{*}\right)^{-1}B_{t+1}^{*}-S_{t}B_{t}^{*}$$
(68)

The risk premium ensures that the economy returns to the steady state¹², thus this variable increases with the foreign debt.

III. CALIBRATION AND DYNAMICS

We choose Chile as our benchmark country for the calibration because it has been a leader within emerging commodity exporters in implementing an acyclical fiscal rule.¹³ Unfortunately, many parameters have never been obtained using Chilean data. For this reason, we calibrate the model taking sensible values from different studies (see Table 1).¹⁴ For example, the discount factor β is 0.99 close to the values found elsewhere in the literature. The risk aversion coefficient σ is greater than one (2.0) as the evidence indicates for small open economies.¹⁵ Thus, the relative prudence coefficient is: $(C_t^0(i) - \psi N_t^0(i)^{\varphi}) U_{CCC} / U_{CC} = -(1 + \sigma) = -3$. This ensures that Ricardian agents will save more as output volatility rises.¹⁶

¹³ The steady state values are consistent with those obtained for the Chilean Economy where foreign debt is around 50 percent of the GDP. See for example Restrepo and Soto (2006).

¹⁴ We assume that each period corresponds to one quarter.

¹⁵ See Agénor and Montiel (1996), Table 10.1, page 353.

¹⁶ For our chosen utility function, there is no closed form solution linking consumption and volatility. An approximation is found in Talmain (1998).

¹¹ We assume for simplicity that there are no private copper exports because these demand no resources. We treat them as if they were transfers from abroad.

¹² See Schmitt-Grohé and Uribe (2003).

The elasticity of substitution across intermediate goods, ε_D and ε_F , is 6, in order to have a mark-up of 20%, the fraction of firms that keep their prices unchanged each period, θ_D and θ_F , is 0.75 and the rate of depreciation δ is 0.025. All these values are standard in the literature on the New Keynesian models (Woodford (2003), Galí and Monacelli (2005) and Galí et al (2007)).

Discount factor (β)	0.99
Risk aversion coefficient (σ)	2.00
Disutility parameters, worked hours (N)	
φ	1 70
ψ	7.02
Weight of rule-of-thumb consumers (λ)	0.50
Rate of depreciation (δ)	0.025
Investment adjustment cost ϕ	1/15
Elasticity of substitution across intermediate goods (ε_D , ε_F)	6.00
Parameter of CES production function (α)	0.40
Fraction of firms that keep their prices unchanged (θ_D, θ_F)	0.75
Real wage mark-up $(1+\theta_W)$	1.20
Elasticity of substitution between capital and labor (σ_s)	1.00
Response of monetary authority to inflation (ϕ_{π})	1.50
Response of monetary authority to output (ϕ_{vr})	0.00
Autoregressive coefficient of copper price	0.80
Share of the production of the natural resource owned by the government (τ_{cu})	0.50
Amount produced of the natural resource (Q^{cu})	0.45
Weight of domestic good in consumption (α_c)	0.60
Weight of domestic good in investment (α_{I})	0.50
Weight of domestic good in government expenditure (α_G)	0.99
Foreign-domestic good (consumption) elasticity of substitution (η_c)	0.99
Foreign-domestic good (investment) elasticity of substitution (η_1)	0.99
Foreign-domestic good (government) elasticity of substitution (η_G)	0.99
Acyclical rule, debt weight (μ_X)	0.01
The share of external public debt over total public debt v_b	0.21
Elasticity of interest rate to external debt	0.001
Elasticity of domestic export to real exchange rate (η^*)	1.00

- 1 1	The second secon	• •	T	
Tabla	Daga	11100	Dorom	otora
Table	DASE	ше	Palall	PIEIS
1 4010	 Dube.		I MIMII	

For the labor market, we suppose the same mark up as in the good market, i.e. θ_w is 0.2. The value of φ (=1.7) comes from Correia et al (1995), who introduced GHH utility function in RBC models for small open economies to explain the higher volatility of the consumption observed in these countries. As they do, we choose a value for ψ (=7.02) to ensure that hours worked in steady state coincide with actual data in our benchmark country. The value of the investment adjustment cost ϕ is 1/15, which is half of the value of Correia et al (1995). Half of households are hand-to-mouth, i.e. λ is 0.5, which is within the range of values considered in other studies (Mankiw (2000) and Galí et al (2007)). We assume that government spending is heavily biased towards domestic goods. Indeed, the share of domestic goods in the government consumption basket α_G is 0.99.

This allows us to replicate a stylized fact: in many commodity exporting countries, increases in government spending cause real appreciations (Edwards, 1989). We do not have information about the values of the elasticity of substitution between domestic and foreign goods (η_c , η_1 , and η_G), thus we assume values close to 1 one (following Galí and Monacelli, 2005). For the same reason we choose values for α_c and α_1 close to 0.5 (also following Galí and Monacelli, 2005) as a measure of openness.

Even though public debt is not exactly zero in Chile, we assume it to be so in our model's steady state. This assumption helps us to compare the acyclical rule with the balanced budget regime: to do so, both policies must share the same steady state. Also, we assume that 21 percent of public debt is held by foreigners ($v_b = 0.21$); this value comes directly from historic Chilean data. In our baseline simulation, the coefficient in the monetary rule with respect to inflation ϕ_{π} is 1.5, which is a standard one for Taylor rules. The interest rate response with respect to the output gap ϕ_{yr} is assumed to be zero. Likewise, the elasticity of substitution between capital and labor σ_s is 1.0. Thus α is the capital share and is assumed to be 0.4 given that this value in Chile is higher than in other countries (in the US, $\alpha = 0.33$). The elasticity of domestic exports to the real exchange rate η^* is 1.0 in line with estimations for developing countries (Ghei and Pritchett (1999)).

The autoregressive coefficient of the real price of copper ρ is 0.8 obtained from quarterly data from 1973 through 2005. We choose small values for the debt weight μ_X (=0.01) in the acyclical rule and the elasticity of the interest rate to external debt (0.001). Both coefficients warrant the stability of the model. The first one makes public debt a stationary variable. The second one forces the current account to be stationary as well as net foreign assets.

IV. EFFECTS OF A COMMODITY (COPPER) PRICE SHOCK

To illustrate how the model economy works under the two extreme alternative fiscal rules, we discuss several shock experiments below. We simulate 100 artificial economies, 1000 period each, hitting the economy with a random shock to the price of copper each period.¹⁷

¹⁷ We also simulated the economy 10.000 periods ahead and the qualitative results did not change.

To begin, Figure 3 shows responses of several macroeconomic variables to one standard deviation (20%) copper price shock.¹⁸ In each of the small charts, the black and grey-blue lines represent impulse responses under balanced budget budget and acyclical structural balance, respectively.

¹⁸ The size of the shock in our simulations is just enough to obtain a standard deviation of the real price of copper similar to the empirical one (33%) for the period 1973-2005.



Figure 3. Responses to a Price of Copper Shock

The balanced-budget rule (black line) yields patterns that are generally procyclical. When copper prices increase, so do government revenues, expenditures, hand-to-mouth private consumption, hours worked, and output. Likewise, the real value of the currency appreciates. Note that, to gauge real appreciation, we look at the relative price of the domestic good P_d/P_m . Since we assume that it is a good proxy for the inverse of the real exchange rate. The real appreciation also reduces non-commodity exports. Inflation rises, as does the real interest rate (via the Taylor rule). Note however, that investment falls: capital expenditures are crowded out by the copper price boom.

By contrast, the acyclical rule (grey-blue line) displays behavior that is less procyclical. By definition, the behavior of government revenues is invariant to regime. However, government spending shows virtually no response to the shock. Instead the public balance is positively related to the copper price shock. GDP and consumption increase only slightly. In addition, the currency shows a much more modest appreciation than under the balanced budget rule, and exports remain largely unchanged. Inflation and interest rates remain unaffected, as does investment; there is no crowding out.

Thus, for most variables, volatility is greater under the balanced budget rule than under the acyclical rule. One important exception to this observation is consumption by Ricardian households, who are able to almost fully neutralize the otherwise volatile effects of government policy.

Some other differences between the rules are shown in Figure 4. An important difference regards evolution of government debt. Under the balanced budget regime government debt is always by definition equal to its initial value, namely zero. By contrast, under the acyclical rule, the government accumulates assets. Over time, average public debt stabilizes: $B^g \approx -30$ percent of GDP. Thus, given that the government can spend the interests received on those asstes average government spending (P^GG) is slightly higher under the acyclical rule than under the balanced budget rule: the government accumulates a "war chest" to help fund expenditures. As mentioned previously, a result like this is discussed in Schmitt-Grohé and Uribe (2004).

As one would expect, consumption by "hand-to-mouth" households C^r differs substantially across regime. Under the acyclical rule, the variability of C^r is substantially lower than under the balanced budget rule. This feature will be critical for our welfare comparisons between rules (below). At the same time, the level of C^r is somewhat higher under the acyclical rule. This reflects the fact that aggregate demand rises under the acyclical regime—a consequence of higher public expenditures, including higher real wages (*W/P*) and employment (*N*), which also help explain higher C^r .

By contrast, consumption by Ricardian households C° does not differ as much across regimes. The variability of C° is somewhat lower under the acyclical regime; Ricardian households are able to neutralize most of the volatility inherent in a balanced budget regime. The level of C° stays flat over time under the acyclical rule but rises slightly under the



Figure 4a. Average of Simulated Series Public debt over GDP,%

balanced budget rule. This reflects different savings and asset accumulation across regimes. Under the balanced budget regime, Ricardian households save more in the initial periods. They build up assets and are hence able to maintain their consumption level.

Quite the opposite, under the acyclical regime, the excessive accumulation of assets of the government causes a decrease in the external debt and then a small decrease in the real interest rate (see Figure 4, especially in the first 300 periods). This will be enough for that the Ricardian households choose to save less: their stock of assets falls, as must their consumption.

In the case of Ricardian households the intuition of the last result is directly related to the precautionary saving motive that is introduced by the second order approximation used to solve the model (see Appendix XX). The Ricardian agents incorporate optimally the variability of the commodity price shock as well. Thus they have a strong precautionary saving motive (measured by the rate of relative prudence), which stimulates the building up of assets when uncertainty is higher. On the contrary, when government follows an acyclical rule, the Ricardian agents will decrease their saving (or increase their debt) for the significant reduction in the volatility of the commodity price that they face. However, this rule leads also the government to save more than what would be optimal from the perspective of the Ricardian agents. Therefore as a result of this strong stabilization of the commodity price impact, these consumers decide optimally to save too little whenever the interest rate goes down so their expected consumption is lower than in the case of a balanced-budget rule.

0.0 79.0 -1.0 251 501 751 78.0 -2.0 77.0 -3.0 -4.0 76.0 -5.0 75.0 -6.0 74.0 -7.0 -8.0 73.0 -9.0 251 501 751 balanced budget rule balanced budget rule acyclical rule acyclical rule Stock of capital Private domestic debt 84.0 3.0 2.5 83.5 2.0 83.0 1.5 82.5 1.0 82.0 0.5 0.0 81.5 -0.5 251 501 751 251 751 501 1 balanced budget rule ---acyclical rule balanced budget rule -acyclical rule Interest payment total private debt Interest payment private domestic debt 0.03 0.09 0.08 0.03 0.07 0.02 0.06 0.02 0.05 0.04 0.01 0.03 0.01 0.02 0.00 0.01 0 751 251 501 -0.01 251 501 751 1 acyclical rule balanced budget rule acyclical rule balanced budget rule

Figure 4b. Average of Simulated Series Financial wealth

Total wealth

V. CALCULATION OF WELFARE LEVELS

A. Methodology

We follow Kollman (2002), Kim and Kim (2003), Elekdag and Tchakarov (2004), Bergin et al (2007) insofar as we also compute the second order approximations developed by Schmitt-Grohé and Uribe (2004) to solve the whole system of equations of the model. In this way, we can include the effect of the volatility on the mean of consumption. Kim and Kim (2003) note, log-linearized business-cycle models are inappropriate for welfare analysis since they are unable to account for the effect of the variance of the shocks on economic decisions.

Thus, we compute the welfare gains generated by moving from one rule to the other, finding the change in steady-state consumption (ξ) required to make any household indifferent (in expected utility terms) between the procyclical balanced budget and the acyclical spending rule. Such a calculation is in the spirit of Robert Lucas (1987). To do so, we start taking unconditional expectations of a second order approximation of expected utility:

$$E[U(C,N)] = E[U(\bar{C},\bar{N}) + U_c(\bar{C},\bar{N})E(C_t - \bar{C}) + \frac{1}{2}U_{cc}(\bar{C},\bar{N})(C_t - \bar{C})^2 + U_n(\bar{C},\bar{N})(N_t - \bar{N}) + \frac{1}{2}U_{nn}(\bar{C},\bar{N})(N_t - \bar{N})^2]$$
(69)

The specific second order approximation of the utility function (equation (3)) is:

$$E[U(C,N)] = \frac{\left(\overline{C} - \psi \overline{N}^{\gamma}\right)^{1-\sigma} - 1}{1-\sigma} + \overline{C}\left(\overline{C} - \psi \overline{N}^{\gamma}\right)^{-\sigma} E(\hat{C}_{t}) - \left(\overline{C} - \psi \overline{N}^{\gamma}\right)^{-\sigma} \psi \gamma \overline{N}^{\gamma} E(\hat{N}_{t}) - \frac{1}{2}\sigma \overline{C}^{2} (\overline{C} - \psi \overline{N}^{\gamma})^{-\sigma-1} \operatorname{var}(\hat{C}_{t}) - \frac{1}{2}\sigma (\overline{C} - \psi \overline{N}^{\gamma})^{-\sigma-1} (\psi \gamma)^{2} \overline{N}^{2\gamma} \operatorname{var}(\hat{N}_{t}) - \frac{1}{2} (\gamma - 1) (\overline{C} - \psi \overline{N}^{\gamma})^{-\sigma} \psi \gamma \overline{N}^{\gamma} \operatorname{var}(\hat{N}_{t})$$
(70)

Note that we use these transformations in the last expression $\hat{X} = \frac{X - \overline{X}}{\overline{X}}$ and therefore $\overline{X}E(\hat{X}) = E(X - \overline{X})$ and $\overline{X}^2V(\hat{X}) = V(X - \overline{X})$. Next, to simplify, we write expected utilities under the procyclical balanced budget and the acyclical spending rule as $E[U(C, N)^{bb}] = \phi_1$ and $E[U(C, N)^{ss}] = \phi_2$, respectively.

Now, note that:

$$E\left[U(C(1+\xi^{unconditional}),N)^{bb}\right] = \frac{\left(\overline{C}(1+\xi^{unconditional})-\psi\overline{N}^{\gamma}\right)^{1-\sigma}-1}{1-\sigma} + (other \ terms)^{bb} = \phi_2$$
(71)

where
$$(other \ term)^{bb} = \phi_1 - \frac{(\overline{C} - \psi N^{\gamma})^{1-\sigma} - 1}{1-\sigma}$$

Thus, the incremental consumption required to equate expected utility across regimes, (ξ) is computed as:

$$\xi^{unconditional} = \frac{\left\{ (1-\sigma) \left[(\phi_2 - \phi_1) + \frac{\left(\overline{C} - \psi \overline{N}^{\gamma}\right)^{1-\sigma}}{1-\sigma} \right] \right\}^{\frac{1}{1-\sigma}} - \left(\overline{C} - \psi \overline{N}^{\gamma}\right)}{\overline{C}}$$
(72)

That is, ξ shows how much additional consumption would be required to make an individual just as well off under a balanced budget regime as under an acyclical spending rule.

The welfare gains of moving from one rule to the other were also computed using conditional measures of utility. This strategy takes into consideration the transition when one of the rules is applied because by computing the discounted sum of expected utilities, it considers the costs of sacrificing consumption for precautionary reasons when the balance budget is put in place (Schmitt-Grohé and Uribe, 2007; Bergin et al 2007).

$$U((1+\xi^{conditional})C,N) = (1-\beta)\sum_{t=0}^{\infty} \beta^{t} E_{o}[U(C,N)]$$
(73)

B. Results

The results of this analysis are shown in Figures 5 and 6. To begin, Figure 5 shows the net welfare gain (measured as a percent of steady state consumption) implied in comparing acyclical versus balanced budget, against the variance of commodity prices.



Figure 5. Welfare Gain (WG) and Variance of Copper Prices $(\sigma_{copper})^*$ Unconditional expectationsConditional expectations

WG: welfare under acyclical minus welfare under balanced budget regime (measured in percent of steady state consumption).

As Figure 4 has already foreshadowed, "hand-to-mouth" consumers benefit from the acyclical rule, not only because their consumption stream is smoother, but also because it is slightly higher. On the other hand, Ricardian consumers loose with this rule. However, the loss computed with the conditional expectation formula is smaller because, as said, it takes into account the consumption foregone whenever the agent is involved in precautionary saving. The right panel in Figure 5 shows that average welfare goes up with the acyclical rule if one weighs both consumers equally.

Figure 5 suggests that the larger the variance of the shock σ_{copper} , the more "hand to mouth" consumption. Figure 6 shows why: as σ^{copper} grows, so does C^r under the acyclical regime, both absolutely and relative to the balanced budget regime. An analogous result holds for government expenditure. Hence, "hand-to-mouth" agents benefit from the (Keynesian) demand stimulus, which results from the acylical spending rule.

By contrast, Ricardian agents suffer somewhat under the acyclical rule relative to the balanced budget rule. Their consumption is slightly less volatile under the acyclical regime (Figure 3). However, in the more volatile balanced-budget environment, Ricardian households build their own precautionary assets, that includes capital stock—from which they are able to later consume. Figure 6 supports these results. It shows that as σ_{copper} grows, the Ricardian agents' consumption C^o under the acyclical rule decreases. Once again, this reflects their lower asset levels that they do not build up in a more certain environment (a lower precautionary savings motive). As a result, their earnings and average consumption decreases over time.



 Figure 6. Difference Between Regimes

 (acyclical minus balanced-budget rule for different commodity price volatilities)

 Private Net Wealth, %
 Consumption Ricardian Agents,%

*Each line is the average of the series that resulted from the simulations with the acyclical spending rule minus those obtained with the balanced-budget rule.

In other words, even though the government has a mechanical acyclical rule it acts as if itself were an agent with a precautionary savings motive: it builds up a prudential asset stock that cushions spending today against shocks while also permitting it to spend more in the future. In turn, this provides a benefical externality for "hand to mouth consumers:" the government is providing a substitute for the precautionary savings that they themselves cannot do. Figure 6 illustrates, under the acyclical rule that the government does what Ricardian consumers would otherwise do under the balanced-budget regime. It accumulates a large amount of assets and ends up with larger revenues and spending. The stock of assets can amount to a large share of GDP if uncertainty increases steadily. Nevertheless, and as we explained in Section 3.2, the mechanical acyclical rule causes an accumulation of assets that is far from being optimal from the perspective of the Ricardian consumers and hence the welfare of this kind of agents is much lower with the acyclical rule.¹⁹

These results also have important implications for the design of a general fiscal rule (see equation 54'). Recall that under a completely acyclical regime, $\alpha_r=0$ and under a balanced budget regime, $\alpha_r = 1$ By contrast, μ_x is a debt targeting parameter: an increase in the value of μ_x implies that the government is targeting more closely the debt stock (the target is the initial value of zero), but with more volatility in government expenditures.²⁰

Table 2 shows the average welfare gains obtained using the conditional expectations for a given volatility of the commodity price shocks, as measured in consumption units for both consumers over a grid of values for μ_x and α_r .

	Table 2. Baseline Parameters								
_	$\alpha_{_{x}}$	0	0.25	0.5	0.75	1			
	0.010	0.1038	0.0981	0.0792	0.0447	0.00			
μ_x	0.033	0.1076	0.1008	0.0810	0.0456	0.00			
	0.055	0.1091	0.1016	0.0828	0.0480	0.00			
	0.078	0.1085	0.1032	0.0831	0.0486	0.00			
	0.100	0.1075	0.1047	0.0861	0.0495	0.00			

Table 2 Deceline Deremeters

¹⁹ Note that the composition of assets is not invariant to the fiscal rule. The acyclical rule encourages more domestic investment in physical capital than the balanced budget. Lower volatility encourages more plant and equipment to be built within the country. By contrast, higher volatility under the balanced budget regime encourages Ricardian consumers to invest abroad due to the precautionary saving motive and the absence of domestic bonds.

²⁰ In a more general context, when target debt b^* is, for example, 50 percent of GDP, a term like μ_x (b_t – b^{*}) would be necessary in the rule.

As one would expect, raising either μ_x or α_r helps Ricardians but hurts hand-to-mouth units. However, raising μ_x is not identical to raising α_r . Table 2 suggests that, if we maintain the acyclical element (keep $\alpha_\tau = 0$) but increase somewhat the debt targeting parameter μ_x , we can benefit Ricardian agents at a very small cost to the hand to mouth agents. But, no such result can be obtained by raising α_r : while Ricardian households always gain, the loss suffered by "hand-to-mouth" households is even greater. Intuitively, α_r is a larger and blunter instrument than μ_x . If μ_x rises, the stock of debt (or assets) must return to zero more quickly than otherwise. If α_r rises, more volatility is introduced directly— through the commodity price channel. By contrast, if μ_x rises, more volatility in introduced but less directly—through the spending channel.

Indeed, we find that, conditional on $\alpha_r = 0$, there is a value of μ_x that maximizes average welfare gains. Therefore, we say that it is the best degree of government spending stabilization. So long as the gain to Ricardian consumers from increasing μ_x exceeds the loss suffered by "hand to mouth" agents, the former can compensate the latter. Note however, that such an optimum will only coincide with one that a social planner would choose for a special case, namely where the social planner's weights on the utility of "hand-to-mouth" and Ricardians coincide *exactly* with the values of λ and $(1-\lambda)$, as defined above. Thus, if the social planner places a weight on "hand-to-mouth" consumers that is greater (less) than l, the optimal value for μ_x will fall (rise).

VI. SUMMARY AND CONCLUSIONS

We assess the welfare implications of reducing the volatility and procyclicality of government expenditures in countries that specialize in a primary resource-based commodity export, facing strong fluctuactions of their fiscal income due to commodity price volatility. Public spending does contribute to aggregate demand (a Keynesian channel) and hence output. Importantly, government expenditure was assumed to be useless. This is so because our focus is to understand under this extreme assumption if there is some role for government spending in stabilizing external shocks and the business cycle.

Our policy, an acyclical spending rule, was geared to helping the most vulnerable "hand-tomouth" consumers. We found that the policy was effective: it provided a substitute financial cushion, hence reducing the volatility of their consumption and increasing welfare. This policy boosted their mean consumption through (Keynesian) aggregate demand channels. However, others in society did not fare so well. "Ricardian" households that were able to optimize over time suffered. Initially, they saved less, a response that we would expect from agents with a precautionary saving motive. Their consumption was slightly less volatile, but over time their average consumption was also less. This result has an intuitive interpretation: effectively, under the acyclical spending rule, government limits what was the role of Ricardian households, namely to smooth consumption and accumulate assets.

An obvious alternative way of increasing consumers' welfare is relaxing one of our modeling assumptions and allowing public spending to be useful. This is equivalent to giving back

part of government spending to the consumers reducing our lump-sum taxes. However, we do not consider this case here.

We found the best degree of spending stabilization by moving slightly away from the perfectly acyclical rule, what increases the welfare of the Ricardian households at a low cost to the hand-to-mouth households. If the asset position of the government is limited through a somewhat more aggressive debt (asset) targeting stance (in our model a slightly higher μ_x); Ricardians saved more initially than before, building up more assets, hence boosting consumption and welfare. In other words, with full capital mobility and financial market participants having access to a wide range of financial instruments, it may be better (welfare reaches a higher level) also include a debt / asset target—even at the expense of extra volatility in expenditures.²¹ We conclude that a largely acyclical rule, in this context, has a positive effect on the welfare of society as a whole depending on how financially restricted consumers are.²²

If policy makers wish to cushion society's most vulnerable agents—those without access to capital markets and who have presumably the lowest wealth, our results show that fiscal policy should de-link public expenditures from current revenues. We conclude that the acyclical rule, in this context, has a positive effect on the welfare of society as a whole depending on how financially restricted consumers are.²³

²³ This paper also touches upon some more general issues in optimal fiscal policy. For example, our optimal debt level is, essentially, a net credit position (in average). This is similar to a conclusion found in Aiyagari et al (2002). In this aspect, our work recognizes that one goal of a government is to provide a financial cushion for "hand-to-mouth" households that are unable to do so for themselves (Tanner and Carey (2005)).

²¹ This could be implemented empirically through infrequent revisions of permanent income and spending.

²² This paper also touches upon some more general issues in optimal fiscal policy. For example, our optimal debt level is, essentially, a net credit position (in average). This is similar to a conclusion found in Aiyagari et al (2002). In this aspect, our work recognizes that one goal of a government is to provide a financial cushion for "hand-to-mouth" households that are unable to do so for themselves (Tanner and Carey (2005)).

References

- Aiyagari, R., Marcet, A., Sargent, T. Seppälä, J., 2002. Optimal Taxation without State-Contingent Debt. Journal of Political Economy 110, 1220–54. Bergin,
- Calvo, G., 1983. Staggered Prices in a Utility Maximizing Framework. Journal of Monetary Economics, 12: 383-98.
- Carroll, C., Kimball, M., 2006. Precautionary Savings and Precautionary Wealth. Mimeo. Entry for the New Palgrave Dictionary of Economics, 2nd Ed.
- Clarida, R., Galí, J., Gertler M., 1999. The Science of Monetary Policy: A New Keynesian Perspective. Journal of Economic Literature 37, 1661-707.
- Correia, I. Neves, J. Rebelo, S., 1995.Business cycles in a Small Open Economy. European Economic Review 39, 1089-1113.
- Edwards, S.1989, Real exchange rates, devaluation, and adjustment, MIT Press
- Elekdag, S., Tchakarov, I., 2004.Balance Sheets, Exchange Rate Policy, and Welfare. International Monetary Fund, IMF Working Papers 04/63.
- Gali, J., T, Monacelli, 2005, Monetary Policy and Exchange Rate Volatility in a Small Open Economy, *Review of Economic Studies*, 72, 707-734.
- Galí, J., López-Salido, J. D., Vallés, J., 2007. Understanding the Effects of Government Spending on Consumption. *Journal of the European Economic Association* 5, 227-70.
- Gavin, M., Perotti, R., 1997. Fiscal Policy in Latin America. NBER Macroeconomics Annual. In: Bernanke, B., Rotemberg, J. (Eds.) NBER Macroeconomics Annual. Cambridge: MIT Press.
- Ghei, N., L. Pritchett, 1999, "The Three Pessimisms: Real Exchange Rates and Trade Flows in Developing Countries," in P. Montiel and L. Hinkle, eds, *Exchange Rate Misalignment: Concepts and Measurement for Developing Countries*, (Oxford and New York: Oxford University Press for the World Bank)
- Greenwood, J., Z. Hercowitz, G. Huffman, 1988, "Investment, Capacity Utilization, and the Real Business Cycle, "*American Economic Review*, v. 78, iss. 3 (June), pp. 402-17
- Hugget, M., Ospina, S., 2001. "Aggregate Precautionary Savings: When is the Third. Derivative Irrelevant,". *Journal of Monetary Economics* 48, 373-396.

Juillard, M., 1996. Dynare: A program for the resolution and simulation of dynamic models

with forward variables through the use of a relaxation algorithm. CEPREMAP. Couverture Orange. 9602.

- Jiménez, J.P., Tromben V., 2006. Política Fiscal en Países Especializados en Productos no Renovables en América Latina. Serie Macroeconomía del Desarrollo 56. Santiago: Naciones Unidas.
- Kaminski, G., Reinhart, C., Végh, C., 2004. When it Rains it Pours: Procyclical Capital Flows and Macroeconomic Policies. In: Gertler, M., Rogoff, K. (Eds.) NBER Macroeconomics Annual. Cambridge: MIT Press, 11-82.
- Kim, J., Kim S., 2003. Spurious Welfare are Reversals in International Business Cycle Models. Journal of International Economics 60, 471-500.
- Kollman, R., 2002. Monetary Policy Rules in the Open Economy: Effects on Welfare and Business Cycles. Journal of Monetary Economics 49, 989-1015.
- Laxton, D., P. Pesenti, 2003, Monetary Rules for Small, Open, Emerging Economies, Journal of Monetary Economics, 50, 1109-1146.
- Lucas R., 1987. Models of Business Cycles, Blackwell.
- Mankiw, G., 2000. The Savers-spenders Theory of Fiscal Policy Shocks?. *American Economic Review* 90, 120-25.
- Restrepo, J.E., Soto C., 2006. Regularidades Empíricas de la Economía Chilena: 1986-2005. *Economía Chilena* 9 ,15-40.
- Richard-Agénor P, P. Montiel, 1996, Development Macroeconomics, Princeton University Press, Princeton, New Jersey
- Schmitt-Grohé, S, Uribe, M., 2003. Closing Small Open Economy Models. *Journal of International Economics* 61, 163-185.
- Schmitt-Grohé, S, Uribe, M., 2004. Solving Dynamic General Equilibrium Models Using a Second-order Approximation to the Policy Function. *Journal of Economic Dynamics* and Control 28, 755-775.
- Schmitt-Grohé, S, Uribe, M., 2007. Optimal Simple And Implementable Monetary and Fiscal Rules with Stephanie Schmitt-Grohe, Journal of Monetary Economics, 54, September 2007, 1702--1725.
- Smets, F., Wouters R., 2002. Openness, Imperfect Exchange Rate Pass-through and Monetary Policy. Journal of Monetary Economics 49, 947-81.

- Talmain, G., 1998. An Analytical Approximate Solution to the Problem of Precautionary Savings. Journal of Economic Dynamics and Control 23, 113–124.
- Talvi, E., Végh C., 2005. Tax Base Variability and Procyclical Fiscal Policy in Developing Countries. Journal of Development Economics 78, 156-190.
- Tanner, E., and K. Carey, 2005. The Perils of Tax Smoothing: Sustainable Fiscal Policy with Random Shocks to Permanent Output. International Monetary Fund Working Paper 05/207..
- Woodford, M., 2003. Interest & Prices: Foundations of a Theory of Monetary Policy. Princeton: Princeton University Press.

Appendix 1: Evaluation of κ

We need to establish the origin of κ from in the numeric simulations. To do so, consider a simplified version of the AC rule, in the first period, spending is equal to revenue since initial debt is assumed to be zero:

$$P_1^G G_1 = IT \tag{1}$$

At the same time spending should obey the government budget constraint:

$$P_1^G G_1 = \overline{IT} + \varepsilon_t + \frac{B_2^G}{R_1}$$
(2)

In the model, the interest rate depends on the level of debt as in Uribe and Schmidt-Grohé: $R_1 = R_1^* (1 + \varpi B_2)$ (3)

Substituting, the rule (1) and the interest rate (3) in the budget constraint (2) the level of debt in the second period can be derived:

$$B_2 = -\frac{\varepsilon R_1^*}{1 + \varepsilon \varpi R_1^*} \tag{4}$$

Assuming that shocks are distributed in such that $\forall t$ there is the same probability of getting a positive or negative shock of equal size *a*

$$\varepsilon_{t} = \begin{cases} a & with \quad probability \quad 0.5 \\ -a & with \quad probability \quad 0.5 \end{cases}$$

It is possible to compute the expected value of the debt level in the second period B_2 :

$$E_1(B_2) = \frac{\varpi(aR_2^*)^2}{1 - (\varpi aR_2^*)^2} > 0 \quad \text{, whenever } \varpi < \frac{1}{aR_1^*}$$

If the expected value of debt is larger than zero, the expected level of spending will be lower $E_1(P_2^G G_2) < \overline{IT}$ because in that case the government will have to pay interest on that debt.

In order for the level of spending to be equal to \overline{IT} , the rule for period one should be:

$$PG_1 = \overline{IT} - \kappa$$

Using the new rule, one can find the new level of B_2 :

$$B_2 = -\frac{(\varepsilon + \kappa)R_2^*}{1 + (\varepsilon + \kappa)\varpi R_2^*}$$

Also, to have expected spending equal to \overline{IT} , the expected level of B_2 should be zero:

$$E_1(B_2) = \left[-\frac{(\kappa - a)\varpi R_1^*}{1 - (\kappa - a)\varpi R_1^*} - \frac{(\kappa + a)\varpi R_1^*}{1 + \varpi(\kappa + a)\varpi R_1^*} \right] = 0$$

Solving for κ :

$$\kappa = \frac{-1 \pm \sqrt{1 + 4\left(a\,\varpi R_1^*\right)^2}}{2\,\varpi R_1^*}$$

The larger the variance of the shocks, the larger κ should be. Note, that only positive values for κ are considered here.

Appendix effect on Ricardian consumers

We can use a informal demonstration to explain why Ricardian consumers have lower consumption in the future with the acyclical rule. Assume that we have two periods and price of copper shock has two possible results as before.

The first order conditions for Ricardian Consumer are Euler equation

$$1 = \beta E_{t} \left(\frac{\left(C_{1}^{0}(i) - \psi N_{1}^{0}(i)^{\varphi} \right)^{\sigma}}{\left(C_{2}^{0}(i) - \psi N_{2}^{0}(i)^{\varphi} \right)^{\sigma}} R_{t} \left(\frac{P_{t}}{P_{t+1}} \right) \right)$$
(1)

and the parity condition.

$$1 = E_t \left(\left(\frac{S_2}{P_2} \right) \left(\frac{P_1}{S_1} \right) \frac{R^* \left(1 + \varpi B_2^* \right)}{R_2 \left(\frac{P_1}{P_2} \right)} \right)$$
(2)

Substituting parity condition into Euler equation we get:

$$1 = \beta E_t \left(\frac{\left(C_1^0(i) - \psi N_1^0(i)^{\varphi} \right)^{\sigma}}{\left(C_2^0(i) - \psi N_2^0(i)^{\varphi} \right)^{\sigma}} \left(\frac{S_2}{P_2} \right) \left(\frac{P_1}{S_1} \right) R^* \left(1 + \varpi B_2^* \right) \right)$$
(1a)

That is equal to:

$$1 = \beta \frac{1}{2} \left(\frac{\left(C_{11}^{0}(i) - \psi N_{11}^{0}(i)^{\varphi}\right)^{\sigma}}{\left(C_{21}^{0}(i) - \psi N_{21}^{0}(i)^{\varphi}\right)^{\sigma}} \right) \left(\left(\frac{S_{21}}{P_{21}}\right) \left(\frac{P_{11}}{S_{11}}\right) R^{*} \left(1 + \varpi B_{21}^{*}\right) \right) \\ + \beta \frac{1}{2} \left(\frac{\left(C_{12}^{0}(i) - \psi N_{12}^{0}(i)^{\varphi}\right)^{\sigma}}{\left(C_{22}^{0}(i) - \psi N_{22}^{0}(i)^{\varphi}\right)^{\sigma}} \right) \left(\left(\frac{S_{22}}{P_{22}}\right) \left(\frac{P_{12}}{P_{22}}\right) R^{*} \left(1 + \varpi B_{22}^{*}\right) \right)$$
(1b)
Where $\beta \frac{1}{2} \left(\frac{\left(C_{1j}^{0}(i) - \psi N_{1j}^{0}(i)^{\varphi}\right)^{\sigma}}{\left(C_{2j}^{0}(i) - \psi N_{2j}^{0}(i)^{\varphi}\right)^{\sigma}} \right) \left(\frac{S_{2j}}{P_{2j}}\right) \left(\frac{P_{1j}}{S_{1j}}\right) R^{*} \left(1 + \varpi B_{2j}^{*}\right)$ is the inverse of marginal utility

multiplied by the interest rate for the "j" state of nature, (j=1 for negative shock and j=2 for positive shock).

Acyclical rule case

Assume for simplicity that all external debt is public. Thus, the decrease in $R^*(1 + \varpi B_{22}^*)$ is bigger (in absolute term) than the increase in $R^*(1 + \varpi B_{21}^*)$. We show informally this in the Appendix 1 where we show that in absolute term $|B_{22}^*| > B_{21}^*$. Therefore we can guess that the effect of the second term of the right hand side is bigger than the first term is.

In other words, in order to hold (1b),
$$\beta \frac{1}{2} \left(\frac{\left(C_{12}^{0}(i) - \psi N_{12}^{0}(i)^{\varphi}\right)^{\sigma}}{\left(C_{22}^{0}(i) - \psi N_{22}^{0}(i)^{\varphi}\right)^{\sigma}} \left(\frac{S_{22}}{P_{22}}\right) \left(\frac{P_{12}}{S_{12}}\right) \right)$$
 must increase
more than the decrease of $\beta \frac{1}{2} \left(\frac{\left(C_{11}^{0}(i) - \psi N_{11}^{0}(i)^{\varphi}\right)^{\sigma}}{\left(C_{21}^{0}(i) - \psi N_{21}^{0}(i)^{\varphi}\right)^{\sigma}} \left(\frac{S_{21}}{P_{21}}\right) \left(\frac{P_{11}}{S_{11}}\right) \right).$

But in the term $\beta \frac{1}{2} \left(\frac{\left(C_{12}^{0}(i) - \psi N_{12}^{0}(i)^{\varphi} \right)^{\sigma}}{\left(C_{22}^{0}(i) - \psi N_{22}^{0}(i)^{\varphi} \right)^{\sigma}} \left(\frac{S_{22}}{P_{22}} \right) \left(\frac{P_{12}}{S_{12}} \right) \right)$ we have that $\left(\frac{S_{22}}{P_{22}} \right) \left(\frac{P_{12}}{S_{12}} \right)$ decreases

because the appreciation occurs in the second period, when government expenditure goes up. Thus one way to increase this terms is that $C_{12}^0 \rangle C_{22}^0$, i.e., present consumption is higher than future consumption when shocks are positive.

The intuition is that when government decides to save a big fraction of the positive shock, Ricardian consumers will hold more public debt if only if interest rate goes down. This happens because $R^*(1 + \varpi B_{22}^*)$ also decreases. Finally, consumers use these resources to increase their present expenditure but they will reduce their consumption in the future because they must pay the debt.

Balanced Budget Rule and the relative prudence coefficient

On the contrary, in the Balanced Budget rules, Ricardian save more for the prudence motivation.

Look again (1b).

$$1 = \beta \frac{1}{2} \left(\frac{\left(C_{11}^{0}(i) - \psi N_{11}^{0}(i)^{\varphi} \right)^{\sigma}}{\left(C_{21}^{0}(i) - \psi N_{21}^{0}(i)^{\varphi} \right)^{\sigma}} \right) \left(\left(\frac{S_{21}}{P_{21}} \right) \left(\frac{P_{11}}{S_{11}} \right) R^{*} \left(1 + \varpi B_{21}^{*} \right) \right) \\ + \beta \frac{1}{2} \left(\frac{\left(C_{12}^{0}(i) - \psi N_{12}^{0}(i)^{\varphi} \right)^{\sigma}}{\left(C_{22}^{0}(i) - \psi N_{22}^{0}(i)^{\varphi} \right)^{\sigma}} \right) \left(\left(\frac{S_{22}}{P_{22}} \right) \left(\frac{P_{12}}{S_{12}} \right) R^{*} \left(1 + \varpi B_{22}^{*} \right) \right)$$

We know that consumers try to smooth their stream of consumption. Thus a positive shocks causes that $R^*(1 + \varpi B_{22}^*)$ decreases and $\beta \frac{1}{2} \left(\frac{\left(C_{12}^0(i) - \psi N_{12}^{-0}(i)^{\varphi} \right)^{\sigma}}{\left(C_{22}^0(i) - \psi N_{22}^{-0}(i)^{\varphi} \right)^{\sigma}} \left(\frac{S_{22}}{P_{22}} \right) \left(\frac{P_{12}}{S_{12}} \right) \right)$ increases.

The contrary happens with a negative shock.

Nevertheless the effects in both terms are not symmetric. Why not? Because this terms $\left(\frac{\left(C_{1_{j}}^{0}(i)-\psi N_{1_{j}}^{0}(i)^{\varphi}\right)^{\sigma}}{\left(C_{2_{j}}^{0}(i)-\psi N_{2_{j}}^{0}(i)^{\varphi}\right)^{\sigma}}\right) \text{ depends on } \sigma \text{ . Therefore, if } \sigma = 2 \text{ , you need that the increase in }$

 C_{12}^0 must be lower that the decrease in C_{11}^0 . In other words, consumers have a bias for saving and this effect is stronger when σ increases. Now remember that the relative prudence coefficient for a GHH function is $(C_t^0(i) - \psi N_t^0(i)^\varphi) U_{CCC} / U_{CC} = -(1 + \sigma)$, thus the bias of saving is caused exclusively due to prudence motivation in the model.

This demonstration shows informally through a simplification of the model that consumers have a bias to increase or maintain consumption in the today respect to the future when fiscal policy is acyclical instead of a balanced budget regime.